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A determination of the gamma-ray flux and photon spectral index distributions of blazars from the *Fermi*-LAT 3LAC

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ABSTRACT

We present a determination of the distributions of gamma-ray photon flux - the so-called LogN-LogS relation – and photon spectral index for blazars, based on the third extragalactic source catalogue of the Fermi Gamma-ray Space Telescope's Large Area Telescope, and considering the photon energy range from 100 MeV to 100 GeV. The data set consists of the 774 blazars in the so-called Clean sample detected with a greater than approximately 7σ detection threshold and located above $\pm 20^{\circ}$ Galactic latitude. We use non-parametric methods verified in previous works to reconstruct the intrinsic distributions from the observed ones which account for the data truncations introduced by observational bias and includes the effects of the possible correlation between the flux and photon index. The intrinsic flux distribution can be represented by a broken power law with a high-flux power-law index of -2.43 ± 0.08 and a low-flux power-law index of -1.87 ± 0.10 . The intrinsic photon index distribution can be represented by a Gaussian with mean of 2.62 ± 0.05 and width of 0.17 ± 0.02 . We also report the intrinsic distributions for the subpopulations of BL Lac and FSRQ (Flat Spectrum Radio Quasar)-type blazars separately and these differ substantially. We then estimate the contribution of FSRQs and BL Lacs to the diffuse extragalactic gamma-ray background radiation. Under the simplistic assumption that the flux distributions probed in this analysis continue to arbitrary low flux, we calculate that the best-fitting contribution of FSRQs is 35 per cent and BL Lacs 17 per cent of the total gamma-ray output of the Universe in this energy range.

Key words: methods: data analysis-galaxies: active-BL Lacertae objects: general-galaxies: jets.

1 INTRODUCTION

In this work we investigate the distributions of gamma-ray photon flux and photon index for the largest flux-limited gamma-ray sample of blazars available at the moment, that of the third extragalactic source catalogue of the *Fermi* Large Area Telescope (LAT) (3LAC – Ackermann et al. 2015a). Most of the extragalactic objects observed by the LAT on the *Fermi Gamma-ray Space Telescope* are classified as blazars (e.g. Abdo et al. 2010b), the active galactic nuclei (AGNs) in which the jet is pointing towards us (e.g. Blandford & Konigl 1979). Characterizing the intensity and spectral characteristics of the gamma-ray emission seen in blazars is an essential for understanding of the physics of the accretion disc and black hole systems in AGNs (e.g. Dermer 2007). Understanding the characteristics of blazars is also crucial for evaluating their contribution to the extragalactic gamma-ray background (EGB) radiation.

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The Fermi-LAT source catalogues are based on observations extending down to gamma-ray energies of 100 MeV. Although the 3LAC reports the photon fluxes in the range 1-100 GeV, the photon flux in the range 100 MeV to 100 GeV is an important quantity for blazars because the most photons are at the lower energies of this range, as are the most photons of the EGB. Therefore, we base this analysis on the full 100 MeV to 100 GeV photon flux, reconstructed as described in Section 2. If the whole 100 MeV to 100 GeV information is used, the threshold flux for detection depends strongly on an object's gamma-ray spectrum. This arises from the energy dependence of the point spread function (Atwood et al. 2009) and is such that harder spectra are detected at lower fluxes. Thus, for determination of the flux distribution one needs to take into account both the flux and the photon spectral index, and that one then deals with a bivariate distribution of fluxes and indexes, which is truncated because of the above-mentioned observational bias. Because the flux detection threshold depends on the photon index, the observed raw distributions do not provide the true LogN-LogS counts or the true distribution of the photon index. Thus a bias free determination of the distributions is more complicated than just counting sources. Here we use non-parametric methods to determine the distributions directly from the data at hand. Other methods such as Monte Carlo have been used, such as in Abdo et al. (2010e) – hereafter MA – and, for example, with redshift information and suitable assumptions the distribution of photon index can be corrected for the bias towards hard spectrum sources as in Venters, Pavildou & Reyes (2009).

In a previous work (Singal, Petrosian & Ajello 2012 - hereafter BP1) we demonstrated the techniques with real and simulated blazar flux and photon index data from the first year Fermi-LAT extragalactic source catalogue (1LAC - Abdo et al. 2010d). As explored by e.g. Petrosian (1992), when dealing with a bi (or more generally multi)-variate distribution, one must determine the correlation (or statistical dependence) between the variables, which cannot be done by simple procedures when the data are truncated. We use a method based on the techniques first developed by Efron and Petrosian (EP; Efron & Petrosian 1992, 1999) which determine the intrinsic correlations (if any) between the variables and then the monovariate distribution of each variable, accounting for the truncations of the data. These techniques have been proven useful for application to many sources with varied characteristics and most recently to the gamma-ray flux and photon index of blazars in BP1 and to radio and optical luminosity in quasars in Singal et al. (2013), where a more thorough discussion and references to earlier works are presented.

In Singal, Ko & Petrosian (2014) we used the spectroscopic redshift information provided for the complete sample of 1LAC Flat Spectrum Radio Quasar (FSRQ)-type blazars to determine the gamma-ray luminosity function, its evolution, and the density evolution for FSRQs. A very similar sample was used with different analysis techniques in Ajello et al. (2012) to obtain the gamma-ray luminosity function and evolution for FSRQs, and a 1LAC-based sample with a combination of measured redshifts and upper and lower limits was used to do the same with BL Lacs in Ajello et al. (2014). However, in the case of 3LAC blazars, the spectroscopic redshift information is incomplete, leading to the utility of this work recovering the intrinsic flux and photon index distributions using the maximal number of well characterized gamma-ray detected blazars of any type.

In this paper we apply these methods to determine the correlation and the intrinsic distributions of flux and photon index of *Fermi*-LAT blazars. In Section 2 we discuss the data used from the 3LAC extragalactic catalogue, and in Section 3 we explain the techniques used and present the results. In Section 4 we describe how the results from such studies are important for understanding the origin of the EGB radiation. A discussion is presented in Section 5.

2 DATA

For this analysis we use the blazar sources reported in the *Fermi*-LAT 3LAC (Ackermann et al. 2015a) that are part of the 'Clean' sample, have a detection test statistic $TS \ge 50$, and which lie at Galactic latitude $|b| \ge 20^{\circ}$. This set of criteria, which has been adopted by the LAT team for certain analyses of the blazar population (e.g. MA), includes those sources that are fully calibrated, removes spurious sources, and maximizes the likelihood of sources being properly identified as to spectral type. The test statistic is defined as $TS = -2 \times (\ln (L_0) - \ln (L_1))$, where L_0 and L_1 are the likelihoods of the background (null hypothesis) and the hypothesis being tested (e.g. source plus background). The significance of a detection is approximately $n \times \sigma = \sqrt{TS}$.

These include 286 which are identified as FSRQ type, 352 which are identified as BL Lacertae (BL Lac) type, and 136 which have



Figure 1. Flux and reported photon spectral index for the 774 *Fermi*-LAT blazars used in this analysis, those with test statistic \geq 50 and $|b| \geq 20^{\circ}$. BL Lac-type blazars (n = 352) are shown as blue triangles, FSRQ-type blazars (n = 286) are shown as red plus signs, and blazars of unidentified or ambiguous type (n = 136) are represented by black ×'s. It is seen that there is a selection bias against soft spectrum sources at fluxes below $\sim 6 \times 10^{-8}$ photons cm⁻² s⁻¹. We also show for a selection of sources (but only a few for clarity) the approximate limiting flux for that source – that is the lowest flux it could have and still be sufficiently bright to be included in the sample given its location on the sky given the reported detection significance. The location of the line used for the truncation boundary is also shown.

uncertain type. This can be compared to the 1LAC with 352 TS ≥ 50 and $|b| \geq 20^{\circ}$ blazars, of which 161 are FSRQs, 163 are BL Lacs, and 28 which are identified as uncertain type. Thus the data set used in this analysis contains more than twice as many blazars as that used in the previous analyses of BP1 and MA. There have also been some blazars that have been reclassified as a different type since the 1LAC, based on e.g. spectral data obtained by Shaw et al. (2012) and Shaw et al. (2013) among other works.

The gamma-ray fluxes in the range 100 MeV to 100 GeV, designated here as F_{100} , and reported photon indexes, are plotted in Fig. 1. The 774 blazars range in F_{100} from 6.01×10^{-10} to 2.10×10^{-6} photons cm⁻² s⁻¹. The photon index Γ is defined such that for the photon spectral density at energy E, $n(E)dE \propto E^{-\Gamma}$ (or the $\nu F_{\nu} \propto \nu^{-\Gamma + 2}$), and is obtained by the LAT collaboration by fitting a power-law to the observed spectra in the above energy interval. In this data set the reported photon index ranges from 1.438 to 3.100. It should be noted that some blazars manifest a photon flux as a function of photon energy in the range 100 MeV to 100 GeV that cannot be completely described by a single power law, showing curvature in the spectrum or other features. However, the 3LAC does report a best-fitting power-law index for every blazar, and this analysis uses that power law.

We recover F_{100} from the reported flux density (*K*), pivot energy (E_p) , and photon index with

$$F_{100} = \int_{100 \,\mathrm{MeV}}^{100 \,\mathrm{GeV}} K \left(\frac{E}{E_{\mathrm{p}}}\right)^{\Gamma} \mathrm{d}E.$$
 (1)

 F_{100} is the blazar gamma-ray flux measure adopted in e.g. MA and is useful for exploring blazars and their relationship to the EGB as discussed in Section 1. We obtain the flux density and the pivot energy for 3LAC blazars from the corresponding general *Fermi* source catalogue (Acero et al. 2015). The bias mentioned above is clearly evident; there is a strong selection against soft spectrum sources at fluxes below $F_{100} \sim 6 \times 10^{-8}$ photons cm⁻² s⁻¹.

Every blazar has an associated TS as discussed above, with the background flux being a function of position on the sky (Abdo et al. 2010d). In Fig. 1 we also show the approximate limiting flux of some (only some to avoid visual confusion) of the blazars, which is an estimate of the lowest flux it could have to be included in the sample, given by $F_{\text{lim}} = F_{100} / \sqrt{\text{TS}/50}$. This F_{lim} will thus have some dependence on the object's photon index and position on the sky. However, as discussed in BP1, since there is some uncertainty in the detection threshold values of fluxes and indexes, the limiting flux as determined in this way is not the optimal estimate. We therefore use a more conservative truncation as shown by the straight line in Fig. 1. As verified with the simulated data discussed in BP1, moving the truncation line to the right and down eliminates more sources in the edges of the sample, and does not change the results but increases the uncertainty, while moving it to the left changes the results. We choose the truncation line boundary that is at the edge of this region where the results are not changed. This way we lose some data points but make certain that we are dealing with a complete sample with a well-defined truncation.

3 DETERMINATIONS OF DISTRIBUTIONS

3.1 Correlations

As discussed in Section 1, with a bivariate truncated data set one must determine whether the variables are independent before considering distributions. If in this case F_{100} and Γ are independent, the combined distribution $G(F_{100}, \Gamma)$ can be separated into two independent distributions $\psi(F_{100})$ and $h(\Gamma)$. However, they may not be independent even though flux clearly depends strongly on redshift while photon index may not, and in fact does not in the case of FSRQs (Singal et al. 2014). Correlations between flux and photon index are observed for example in gamma-ray bursts (Lloyd, Petrosian & Mallozzi 2000; Yonetoku et al. 2004). There may also be an observed correlation induced by the selection biases, as there certainly is in this case as can be seen in Fig. 1, which should be removed in order to obtain bias free distributions of the variables. Thus, the first task is to establish whether the variables are independent.

While the flux and photon index exhibit a strong correlation in the raw (and heavily biased) data, determining the intrinsic correlation when the data are truncated requires statistical methods to account for the missing data. In BP1 we discuss in detail the methods we apply to the bivariate *Fermi*-LAT observational blazar data. We use a technique first explored by EP (Efron & Petrosian 1992, 1999) to determine whether the two variables are correlated. This method utilizes a modified version of the Kendall Tau test with the test statistic

$$\tau = \frac{\sum_{j} (\mathcal{R}_{j} - \mathcal{E}_{j})}{\sqrt{\sum_{j} \mathcal{V}_{j}}}$$
(2)

to quantify the independence of two variables in a data set, say (x_j, y_j) for j = 1, ..., n. Here \mathcal{R}_j is the dependent variable (y) rank of the data point *j* in a set associated with it. For untruncated data (i.e. data truncated parallel to the axes) the set associated with point *j* includes all of the points with a lower (or higher) independent variable value $(x_k < x_j)$. If the data are truncated the unbiased set is then the *associated set* consisting only of those points of

lower (or higher) independent variable (x) value that would have been observed if they were at the x value of point j given the truncation.

If (x_j, y_j) are uncorrelated then the ranks of all of the points \mathcal{R}_j in the dependent variable within their associated set should be distributed uniformly between 0 and the number of points n, with the rank uncorrelated with their independent variable value, with the expectation value $\mathcal{E}_j = (1/2)(n + 1)$ and variance $\mathcal{V}_j = (1/12)(n^2 - 1)$, where n is the number of objects in object j's associated set. Then the points' contributions to τ will tend to sum to zero. On the other hand, if the independent and dependent variables are correlated, then the rank of a point in the dependent variable will be correlated with its independent variable, and because the set to be ranked against consists of points with a lower independent variable value, the contributions to τ will not sum to zero.

Independence of the variables is rejected at the $m\sigma$ level if $|\tau| > m$, and this can be considered the same standard deviation as would be calculated from another method such as least-squares fitting, as discussed in Efron & Petrosian (1999). If the variables are not independent, to find the best-fitting correlation the y data are then adjusted by defining some new dependent variable $y'_j = F(y_j, x_j)$ and the rank test is repeated, with different values of parameters of the function *F*.

To determine the intrinsic correlation between F_{100} and Γ we use a function which is a simple coordinate rotation, defining a new variable we call the 'correlation reduced photon index' as

$$\Gamma_{\rm cr} = \Gamma - \beta \times \log\left(\frac{F_{100}}{F_0}\right). \tag{3}$$

Then we determine the value of the parameter β empirically that makes F_{100} and Γ_{cr} independent. This is the best-fitting value of the correlation between F_{100} and Γ for this functional form. The distributions of F_{100} and Γ_{cr} are indeed separable:

$$G(F_{100}, \Gamma) = \psi(F_{100}) \times \hat{h}(\Gamma_{\rm cr}).$$
(4)

Once the monovariate distributions of F_{100} and Γ_{cr} are determined then the true distribution of Γ can be recovered by an integration over F_{100} as:

$$h(\Gamma) = \int_{F_{100}} \psi(F_{100}) \,\hat{h}\left(\Gamma - \beta \times \log\left(\frac{F_{100}}{F_0}\right)\right) \,\mathrm{d}\,F_{100}.\tag{5}$$

Here F_0 is some fiducial flux we chose to be $F_0 = 6 \times 10^{-8}$ photons s⁻¹ cm⁻² sr⁻¹ which is approximately where the flux distribution breaks (see below), although its actual value is not important – it is simply utilized to avoid taking the logarithm of a dimensionless number. The data described in Section 2 are truncated in the F_{100} - Γ plane, due to the bias against low flux, soft spectrum sources. As discussed in Section 2 we can use a curve approximating the truncation, $\Gamma_{\rm lim} = g(\log F_{100})$, which defines the associated set for each point as those objects whose photon index is less than the limiting photon index of the object in question given the truncation curve and its specific value of F_{100} .

As discussed in BP1 we have tested this procedure using a simulated data set from the *Fermi*-LAT collaboration that resemble the real observations and are subject to a truncation similar to the actual observational data, but with known input distributions of uncorrelated photon index and flux. Note that when defining new variables the truncation curve as a function of flux should also be transformed



Figure 2. Test statistic τ versus intrinsic correlation factor β for a photon index and flux correlation of the form given in equation (3), for the 3LAC blazars (solid curve), the subset of BL Lac type blazars (dashed curve), and the subset of FSRQs type blazars (dash-dotted curve). The 1σ range of best-fitting values for β are where $|\tau| \leq 1$. For comparison, the dotted curve shows the correlation factor for just those sources above 6×10^{-8} photons cm⁻² s⁻¹, where the data truncation in the F_{100} , Γ plane is not as relevant.

by same parameter β ;

$$\Gamma_{\rm cr,lim} = \Gamma_{\rm lim} - \beta \times \log\left(\frac{F_{100}}{F_{100-\rm min}}\right). \tag{6}$$

Fig. 2 shows the value of the test statistic τ as a function of the correlation parameter β for all blazars and the subsets including only BL Lacs and FSRQs in the sample. Table 1 shows the best-fitting values and 1σ ranges of the correlation parameter β for these cases. We note that the correlation is generally small, for example for all *Fermi* blazars the best-fitting value is $\beta = -0.13 \pm 0.06$, but significant. This is not surprising, as there is some evidence of an inverse correlation between blazar luminosity and photon index (Ajello et al. 2014). In Singal et al. (2014) we found no evidence

of significant evolution of photon index with redshift for the case of FSRQs, so the result of a possible negative correlation seen here between photon index and flux would indicate that the (small) intrinsic correlation is actually indeed between photon index and luminosity.

3.2 Distributions

With the correlation removed the independent distributions $\psi(F_{100})$ and $\hat{h}(\Gamma_{\rm cr})$ can be determined using a method outlined in Petrosian (1992) based on techniques first devised by Lynden-Bell (1971). These methods give the cumulative distributions by summing the contribution from each point without binning the data, and as discussed in Lynden-Bell (1971), are equivalent to the maximum likelihood distributions.

3.2.1 Flux distributions

For the flux, the cumulative distribution

$$\Phi(F_{100}) \equiv \int_{F_{100}}^{\infty} \psi(F'_{100}) \,\mathrm{d}F'_{100} \tag{7}$$

is obtained with

$$\Phi(F_{100}) = \prod_{j} \left(1 + \frac{1}{N(j)} \right),\tag{8}$$

where *j* runs over all objects with fluxes $F_{100,j} \ge F_{100}$, and N(j) is the number of objects *i* in the *associated set* of object *j* that have a value of $F_{100,i} \ge F_{100,j}$. The associated set for object *j* in this case is all of those objects that have $\Gamma_{cr} \le \Gamma_{cr,lim}(F_{100,j})$, determined from the truncation curve described above. Equation (8) represents the established Lynden-Bell method which we modify by including only those objects within object *j*'s associated set for the calculation of N(j). The use of only the associated set for each object removes the biases introduced by the truncation in this calculation.

We determine the differential flux distribution

$$\psi(F_{100}) = -\frac{\mathrm{d}\Phi(F_{100})}{\mathrm{d}F_{100}} \tag{9}$$

Table 1. Best-fitting parameters for *Fermi*-LAT blazar intrinsic distributions, as calculated in this work, and two analyses with the smaller *Fermi*-LAT 1LAC – ours (BP1 – Singal et al. 2012) and MA (Abdo et al. 2010e).

σ^{f}
0.17 ± 0.02
0.25 ± 0.03
0.28 ± 0.01
0.18 ± 0.03
0.24 ± 0.02
0.23 ± 0.01
0.19 ± 0.02
0.17 ± 0.02
0.18 ± 0.01

Notes. ^{*a*}The correlation between photon index Γ and log flux F_{100} . See equation (3) and Section 3.1. A higher value of β (i.e. more positive correlation between flux and photon index absolute value) moves the mean of the photon index distribution down to lower photon index absolute value (lower μ) and makes the faint end source counts slope less steep (less negative m_{below}), while a lower value of β has the opposite effect.

^{*b*}The power law of the intrinsic flux distribution $\psi(F_{100})$ at fluxes above the break in the distribution. See equation (10). All values reported for this work include the full range of results and their uncertainties when considering the 1σ range of β .

^cThe flux at which the power-law break in $\psi(F_{100})$ occurs, in units of 10^{-8} photons cm⁻² s⁻¹. We present the value even though the precise location of the break is not important for the analysis in this work.

^dThe power law of the intrinsic flux distribution $\psi(F_{100})$ at fluxes below the break. See equation (10).

^{*e*}The mean of the Gaussian fit to the intrinsic photon index distribution $h(\Gamma)$.

^{*f*}The 1 σ width of the Gaussian fit to the intrinsic photon index distribution $h(\Gamma)$.

^gIncluding all FSRQs, BL Lacs, and those of unidentified type.



Figure 3. Observed (diamonds) and reconstructed intrinsic (stars) differential distribution of gamma-ray flux $\psi(F_{100})$ for the 3LAC *Fermi*-LAT blazars. The vertical error bars on the stars represent the 1σ range of the correlation parameter β , the dominant source of uncertainty, and are generally smaller than the points. The intrinsic distribution is a power law with a break at $F_{\rm br} \simeq 8 \times 10^{-8}$ photons cm⁻² s⁻¹. The best-fitting slopes for the intrinsic distribution are -2.43 ± 0.08 above the break and -1.87 ± 0.10 below, and the best-fitting intrinsic distribution is plotted as the dotted line. We also plot the best-fitting $\psi(F_{100})$ as determined in BP1 (small crosses) and MA with error bars (dotted lines). The best-fitting value for $\psi(F_{\rm break})$ is $1.66 \times 10^8 \, {\rm sr}^{-1} F_{100}^{-1}$. The distribution parameters for the BL Lac and FSRQ subpopulations separately are presented in Table 1.

by fitting piecewise polynomial functions via least-squares fitting to $\Phi(F_{100})$ and calculating the derivatives. Fig. 3 shows the calculated intrinsic differential distribution $\psi(F_{100})$, along with those obtained from the raw observed data without correcting for the bias. A direct comparison to the results from BP1 and MA is presented there as well. For consistency with earlier works such as MA we fit the differential counts as a broken power law which describes the data well and takes the form

$$\psi(F_{100}) = \psi(F_{\text{break}}) \left(\frac{F_{100}}{F_{\text{break}}}\right)^{m_{\text{above}}} \text{ for } F_{100} \ge F_{\text{break}}$$
$$\psi(F_{\text{break}}) \left(\frac{F_{100}}{F_{\text{break}}}\right)^{m_{\text{below}}} \text{ for } F_{100} < F_{\text{break}}.$$
(10)

 m_{above} and m_{below} are the power-law slopes above and below the break, respectively, and are obtained from a least-squares fitting of $\psi(F_{100})$, as is the value of F_{break} . At values of F_{100} above $F_{NT} \equiv 6 \times 10^{-8}$ photons cm⁻² s⁻¹ the truncation imposed by the boundary line shown in Fig. 1 is not significant and we can obtain the normalization by scaling the cumulative distribution $\Phi(F_{100})$ such that

$$\Phi(F_{NT}) = \frac{N \pm \sqrt{N}}{8.26 \,\mathrm{sr}},\tag{11}$$

where *N* is the number of objects above F_{NT} in the data set in question and is equal to 89 for all blazars, 20 for BL Lacs, and 65 for FSRQs. The \sqrt{N} uncertainty arises because of Poisson noise for the brightest sources, and 8.26 sr is the total sky coverage considered, which is $|b| \ge 20^{\circ}$ as discussed in Section 2. This normalization then allows the properly normalized value of $\psi(F_{\text{break}})$ to be calculated. The best-fitting value for $\psi(F_{\text{break}})$, corresponding to the best-fitting value of m_{above} is then $1.2 \times 10^8 \text{ sr}^{-1} F_{100}^{-1}$.



Figure 4. Observed (diamonds) and reconstructed intrinsic (stars) distribution of photon index $h(\Gamma)$ for the 3LAC *Fermi*-LAT blazars used in this analysis. The intrinsic distribution is calculated from the flux distribution and the correlation reduced photon index distribution by equation (5). The stars represent the intrinsic distribution calculated with the best-fitting value of the correlation parameter β and the solid curve is the best-fitting Gaussian function to these values, while the dotted curves represent the best-fitting Gaussian functions to the extremal intrinsic distributions allowed by the 1σ range of β . The intrinsic distribution can be represented by a Gaussian with a mean of 2.62 ± 0.05 and 1σ width of 0.17 ± 0.02 , while the raw observed distribution can be represented by a Gaussian with a mean of 2.19 ± 0.01 and 1σ width of 0.34 ± 0.01 . The normalization of $h(\Gamma)$ is arbitrary.

3.2.2 Photon index distributions

To determine the cumulative distribution of the correlation reduced photon index

$$\hat{P}(\Gamma_{\rm cr}) \equiv \int_0^{\Gamma_{\rm cr}} \hat{h}(\Gamma_{\rm cr}') \,\mathrm{d}\,\Gamma_{\rm cr}'$$
(12)

we use

$$\hat{P}(\Gamma_{\rm cr}) = \prod_{k} \left(1 + \frac{1}{M(k)} \right) \tag{13}$$

in the modified method of Lynden-Bell (1971) as above, which can be differentiated to give the differential distribution

$$\hat{h}(\Gamma_{\rm cr}) = \frac{\mathrm{d}\hat{P}(\Gamma_{\rm cr})}{\mathrm{d}\,\Gamma_{\rm cr}}.\tag{14}$$

In this case, *k* runs over all objects with a value of $\Gamma_{cr,k} \leq \Gamma_{cr}$, and M(k) is the number of objects *i* with $\Gamma_{cr,i} \leq \Gamma_{cr,k}$ in the *associated* set of object *k*. Here the associated set for object *k* is those objects with $F_{100} \geq F_{\lim,k}$ obtained from the truncation line at $\Gamma_{cr,k}$. We note again that the cut-off curve as a function of flux is scaled by β in the same manner of equation (3).

 $\hat{h}(\Gamma_{cr})$ can be used via equation (5) to obtain the intrinsic distribution of the photon index itself, $h(\Gamma)$. The results are shown in Fig. 4 along with the raw observed distribution for comparison. Because the mean of intrinsic distribution of photon index is sensitive to the value of the correlation parameter β , we include the full range of intrinsic distributions resulting from the 1σ range of β . A Gaussian form provides a good description of the intrinsic distribution of the index.

We have carried out the same procedures to obtain the distributions of the BL Lac and FSRQ subsets of the data. Table 1 summarizes the best-fitting parameters for the intrinsic flux and photon index distributions, for the sample considered as a whole, and for the BL Lac and FSRQ subpopulations separately. The errors reported include statistical uncertainties in the fits and the deviations resulting from the 1σ range of the correlation parameter β , with the latter being much larger in magnitude. A higher value of β (i.e. more positive correlation between flux and photon index absolute value) moves the mean of the photon index distribution down to a lower absolute value of the photon index and makes the faint end source counts slope less steep (less negative m_{below}), while a lower value of β has the opposite effect.

4 TOTAL OUTPUT FROM BLAZAR POPULATIONS AND THE EGB

One can integrate the flux distribution to calculate the total flux from a population and its proportional contribution to a photon background. In this case, we are interested in the EGB, defined here as the total extragalactic gamma-ray photon output.¹ In BP1 we focused on using the flux distribution to estimate the contribution from blazars as a whole. Here with a much larger sample we will use the flux distributions to estimate the FSRQ and BL Lac contributions separately. The total output in gamma-ray photons from blazar sources with fluxes greater than a given flux F_{100} , in terms of photons s⁻¹ cm⁻² sr⁻¹ between 0.1 and 100 GeV, is

$$\mathcal{I}_{\gamma}(>F_{100}) = \int_{F_{100}}^{\infty} F_{100}' \psi(F_{100}') \,\mathrm{d}F_{100}'. \tag{15}$$

Integrating by parts the contribution to the EGB can be related directly to the cumulative distribution $\Phi(F_{100})$ which is the primary output of our procedure

$$\mathcal{I}_{\gamma}(>F_{100}) = F_{100} \Phi(F_{100}) + \int_{F_{100}}^{\infty} \Phi(F_{100}') \,\mathrm{d}F_{100}'. \tag{16}$$

The advantage of using the latter equation is that it can give a stepby-step cumulative total contribution to the background instead of using analytic fits to the differential or cumulative distributions obtained from binning the data. Fig. 5 shows $\mathcal{I}_{\gamma}(>F_{100})$ for FSRQs and BL Lacs *at fluxes probed by this analysis*. Note that this includes the contribution from both detected blazars and some of those undetected owing to the truncation in the F_{100} , Γ plane but still probed by the analysis. Therefore, this calculated contribution can be more than the total contribution of blazars resolved by *Fermi*-LAT in the 3LAC.

In order to estimate the contribution of objects at fluxes *not* probed by the *Fermi*-LAT to the total EGB one can extrapolate the flux distribution we have obtained to lower fluxes. This extrapolation is more uncertain. We fit a power law to the faint end of the $\Phi(F_{100})$ distributions so that we can extend the integration of equation (16) to lower fluxes. Integrating to zero flux we find that FSRQs would produce a photon output of $\mathcal{I}_{\gamma}(>F_{100}=0) = 3.6$ $(+3.4/-0.9) \times 10^{-6}$ photons s⁻¹ cm⁻² sr⁻¹ and BL Lacs would produce a photon output of $\mathcal{I}_{\gamma}(>F_{100}=0) = 1.8$ $(+4.5/-0.5) \times 10^{-6}$ photons s⁻¹ cm⁻² sr⁻¹. These relatively large ranges are due to the uncertainty in the faint end cumulative source counts slope, ultimately owing to the range of the correlation parameter β , where the best-fitting value reported is for the middle of the 1σ faint end slope of $\Phi(F_{100})$.





Figure 5. Estimate of the cumulative number of photons between 0.1 and 100 GeV above a given F_{100} , $\mathcal{I}_{\gamma-\text{pop}}(>F_{100})$ from equation (16), from FS-RQs (red upper points) and BL Lacs (blue lower points), shown with error bars resulting from the 1σ range of the correlation parameter β . The error bars are generally smaller than the plotting symbols used, except for the leftmost points. The dashed horizontal line shows the EGB, i.e. the total extra-galactic gamma-ray output (\mathcal{I}_{EGB}) as defined here. An estimated total contribution of a population to \mathcal{I}_{EGB} can be obtained by integrating equation (16) to zero flux, as discussed in Section 4.

This is to be compared with the total observed EGB, consisting of unresolved emission plus resolved sources, of $\mathcal{I}_{EGB} = 10.4 \times 10^{-6}$ photons s⁻¹ cm⁻² sr⁻¹ reported by *Fermi* (Ackermann et al. 2015b). It should be noted that this represents a change from the previous *Fermi* estimate of $\mathcal{I}_{EGB} = 14.4 \pm 1.9 \times 10^{-6}$ photons s⁻¹ cm⁻² sr⁻¹ (Abdo et al. 2010a). *If* the populations continue to have the fitted power-law distribution to zero flux then FSRQs would produce 35(+35/-9) per cent of the observed EGB and BL Lacs would produce 17(+44/-12) per cent.

These results are roughly consistent with a number of other findings. In Singal et al. (2014) we consider redshift evolution effects with a smaller sample with complete available spectroscopic redshifts and find that for FSRQs the contribution to the EGB is 22(+10/-4) per cent, with the result as reported here scaled by a factor of 1.38 for the ratio of the higher previously reported *Fermi* EGB intensity to the new recently reported lower intensity, while Ajello et al. (2012) report 30.1(+2.5/-1.7) per cent for FSRQs with the result as reported here likewise scaled. For BL Lacs, Ajello et al. (2014) estimate that they contribute between 14 and 20 per cent of the EGB with the same scaling.² However, comparing the results obtained here from a large sample but with only flux information to those considering smaller samples with redshift evolution information can be enlightening, as discussed in Section 5.

We note that blazars should not be present to arbitrarily low flux so the integration here to zero flux is an overestimate in particular for the high ranges of the above estimates which are most sensitive to the low flux integration limit. The best-fitting values obtained here do not favour blazars being the sole significant contributor to the EGB. Several authors (e.g. Stecker & Venters 2011; Abazajian, Branchet & Harding 2012) have suggested that blazars could be the primary source of the EGB. The spectral index of the EGB of ~2.4 (Abdo et al. 2010a) is consistent with the mean photon index of the

² The original reported numbers are 16(+10/-4) per cent for FSRQs from BP1, 21.7(+2.5/-1.7) per cent for FSRQs from Ajello et al. (2012), and 10–15 per cent for BL Lacs from Ajello et al. (2014).

blazars as determined in BP1 and in MA (although less so with the mean photon index determined here). In a similar vein, Venters & Pavildou (2011) have shown that the spectrum of the EGB is consistent with a blazar origin. Other possible source populations include star-forming galaxies, which have been recognized as a possible major contributor to the EGB by e.g. Stecker & Venters (2011), Fields, Pavildou & Prodanović (2010), and Lacki et al. (2011), although this has been disputed by Makiya, Totani & Kobayashi (2011), radio galaxies (e.g. Inoue 2011), and other non-blazar AGN (e.g. Inoue & Totani 2009, 2011). Additional arguments against blazars being the sole significant contributor to the EGB have been made based on the observed EGB anisotropy in Cuoco, Komatsu & Siegal-Gaskins (2012) and Harding & Abazadjian (2012).

5 DISCUSSION

We have applied a method to calculate the intrinsic distributions in flux and photon index of blazars directly from the observed Fermi-LAT 3LAC catalogue without reliance on simulations. This method accounts for the pronounced data truncation introduced by the selection biases inherent in the observations when the full 100 MeV to 100 GeV observational range is used, and addresses the possible correlation between the variables. The accuracy of the methods used here when applied to Fermi-LAT blazar flux and photon index data were demonstrated in the appendix of BP1 using a simulated data set with known distributions. A summary of the best-fitting correlations between photon index and flux, and the best-fitting parameters describing the inherent distributions of flux and photon index, are presented in Table 1 along with the values obtained in BP1 with the smaller 1LAC data set and by MA. We have obtained the intrinsic distributions considering the major data truncation arising from Fermi-LAT observations. More subtle issues affecting the distributions we have derived, especially the photon index distribution, may arise due to the finite bandwidth of the Fermi-LAT and lack of complete knowledge of the objects' spectra over a large energy range and deviations from simple power laws. However the Fermi-LAT bandwidth is sufficiently large that the contribution of sources which peak outside of this range to the source counts and the EGB in this energy range will be small.

A limitation of these results is the use of the reported best-fitting power-law photon index for each blazar, even though some, or perhaps most, sources actually deviate from a strict power law in the relation between photon flux and photon energy. According to Ackermann et al. (2015a) a total of 91 FSRQs, 32 BL Lacs, and 8 blazars of unknown type in the 3LAC show significant curvature in their spectra. As shown in that paper it is overwhelmingly the highest TS (and therefore generally higher flux) blazars which have been shown to have significant curvature away from a true power law in this relationship. Spectral curvature could be a property of the higher flux blazars, or possibly more likely it is a general feature of blazars which has been most readily observable in those blazars with the highest TS. If the former is the case, then the effect on the truncation and issues related to the truncation would be minimal no matter how the truncation is dealt with. However, even in the case of the later, since this analysis relies on an empirical curve to approximate the truncation in the reported F_{100} , Γ plane as discussed in Section 3.1, the analysis itself should not be particularly sensitive to deviations from a strict power law. However, to the extent that power laws are not representative of the true spectral properties of bright blazars in the energy range 100 MeV to 100 GeV, that will be the case in these results and the distributions of photon index must be understood to be distributions of the best-fitting power-law photon index. As stated in Abdo et al. (2010c), 'Although some spectra display significant curvatures, the photon index obtained by fitting single power-law models over the whole LAT energy range provides a convenient means to study the spectral hardness.'

In section 3.2 of BP1 we consider the uncertainties and errors present in this analysis resulting from individual measurement uncertainties, blazar variability, and source confusion. We conclude that the errors and uncertainties introduced from each of these effects are small compared to the dominant source of uncertainty in this analysis, which is that arising from the range of the correlation parameter β which propagates through every other determination. As we argue in **BP1**, to the extent that faint blazars are more likely to be observed by instruments such as the Fermi-LAT if they are in the flaring state rather than the quiescent state (e.g. Stecker & Salamon 1996), then the observed blazars should have a different mean photon index than the EGB, were the EGB to be made primarily from quiescent state blazars, under the assumption that blazars in the flaring state have a different spectrum than in the quiescent state. As the reconstructed mean photon index here (and elsewhere) of the *Fermi*-LAT observed population is close to (although not exactly) that of the EGB, and there is only a weak relation and correlation between flux and photon index, this would imply that at least one of the following must be the case: (a) there is not a significant bias in the Fermi-LAT towards detecting blazars in the flaring state; (b) quiescent blazars do not form the bulk of the EGB; or (c) flaring and quiescent blazars have, en masse, roughly the same photon index distributions.

We find that the photon index and flux show a slight negative correlation. This correlation is greater than 1σ significance for all blazars, and is quite significant in the case of the FSRQ subpopulation. This correlation likely results from an underlying correlation between photon index and luminosity, as discussed in Section 3.1. Viewing the flux and photon index distributions, the comparison of the intrinsic and raw observed distributions show clearly the substantial effects of the observational bias, as can be seen in Figs 3 and 4. The intrinsic differential counts can be fitted adequately by a broken power law and the photon index appears to have an intrinsic Gaussian distribution.

We also find that in general the values reported here are consistent with those reported in BP1 and MA for the power-law slopes of the flux distribution $\psi(F_{100})$ above the breaks and the distributions of photon index $h(\Gamma)$. The allowed range of the correlation parameter β here and in **BP1** allows for wider uncertainty in these values in some cases than in MA. However, as expected, the uncertainty is generally lower here than in BP1, as this sample has roughly twice as many sources. We note that in this work we find systematically steeper power-law slopes of the flux distribution $\psi(F_{100})$ below the breaks than in BP1 and MA. The differences with MA are significant although the differences with **BP1** are not significant at the 1σ level due to the larger uncertainties. We also note that the best-fitting widths of the Gaussian fits to the photon index distributions are systematically smaller here than in BP1 and MA for the cases of all blazars and BL Lacs, but not for FSRQs, and that the mean photon index for all blazars found here is higher than in the other works, and this is entirely the result of the mean photon index for FSRQs being higher.

Using the bias free flux distributions we calculated the integrated contribution of FSRQs and BL Lacs to the EGB as a function of flux. We obtain this directly from the cumulative flux distribution which is the main output of the methods used. Using the simplistic assumption that the distributions continue unchanged to arbitrarily low flux, the best-fitting contribution of FSRQs and BL Lacs to the total extragalactic gamma-ray radiation in the range 0.1-100 GeV is estimated to be 35 and 17 per cent, respectively. The significant uncertainties reported here for the source count slopes and the estimated contribution of blazars to the EGB are ultimately due to the allowed range of the correlation parameter β , as discussed at length in BP1. These results for the proportional contribution to the EGB are roughly consistent with a number of other findings. In Singal et al. (2014) we consider redshift evolution effects with a smaller sample with available redshifts and find that for FSRQs the contribution to the EGB is 22(+10/-4) per cent, while Ajello et al. (2012) report 30.1(+2.5/-1.7) per cent for FSRQs and Ajello et al. (2014) estimate that BL Lacs contribute between 10 and 15 per cent of the EGB, with all of these reported here scaled to account for the subsequently reduced estimated level of the EGB as discussed in Section 4. However, we note that one would not necessarily expect exact agreement between the estimates of total photon output derived here extrapolating the flux distributions to arbitrarily low flux and those derived considering the full redshift evolutions, for two primary reasons. One is that as the populations clearly have both luminosity and density evolution in redshift (e.g. Ajello et al. 2012, 2014; Singal et al. 2014), one would not expect the flux distribution to remain constant at lower fluxes. The other is that blazars likely do not continue to arbitrarily low flux; indeed in BP1 we argue that a reasonable lower cut-off flux for blazars would be around $\sim 10^{-12}$ photons $cm^{-2} s^{-1}$. The fact that we do find reasonable agreement between the estimates here and those arrived at considering redshift evolutions indicates not only that analyses seem to be consistent, but also that there may be a 'conspiracy' where luminosity and density evolution effects, as well as an absolute luminosity cut-off for blazars, and any effects from contributions missed here because some 17 per cent of 2 LAC blazars are of unclassified type, sum in such a way as to render extrapolations of the distributions recovered here to arbitrarily low fluxes appropriate. It also points to the utility of comparing this analysis, which is based on the statistically larger 3LAC sample which is the largest extant sample of gamma-ray detected blazars, with those of smaller samples that contain complete redshift information.

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REFERENCES

Abazajian K., Branchet S., Harding J., 2012, Phys. Rev. D, 85, 043509 Abdo A. et al., 2010a, Phys. Rev. Let., 104, 101101 Abdo A. et al., 2010b, ApJS, 188, 405

- Abdo A. et al., 2010c, ApJ, 710, 1271
- Abdo A. et al., 2010d, ApJ, 715, 429
- Abdo A. et al., 2010e, ApJ, 720, 435 (MA)
- Acero F. et al., 2015, ApJS, 218, 23
- Ackermann M. et al., 2015a, ApJ, 810, 14
- Ackermann M. et al., 2015b, ApJ, 799, 86
- Ajello M., Shaw M., Romani R., Dermer C., Costamonte L., King G., Max-Moerbeck W., 2012, ApJ, 751, 108
- Ajello M. et al., 2014, ApJ, 780, 73
- Atwood W. et al., 2009, ApJ, 697, 1071
- Blandford R., Konigl A., 1979, ApJ, 416, 450
- Cuoco A., Komatsu E., Siegal-Gaskins J. M., 2012, Phys. Rev. D, 86, 063004
- Dermer C., 2007, ApJ, 654, 958
- Efron B., Petrosian V., 1992, ApJ, 399, 345
- Efron B., Petrosian V., 1999, J. Am. Stat. Assoc., 94, 824
- Fields B., Pavildou V., Prodanović T., 2010, ApJ, 722, L199
- Harding J. P., Abazajian K. N., 2012, J. Cosmol. Astropart. Phys., 11, 26
- Inoue Y., 2011, ApJ, 733, 66
- Inoue Y., Totani T., 2009, ApJ, 702, 523
- Inoue Y., Totani T., 2011, ApJ, 728, 73
- Lacki B., Thompson T., Quataert E., Loeb A., Waxman E., 2011, ApJ, 734, 107
- Lloyd N., Petrosian V., Mallozzi R., 2000, ApJ, 534, 227
- Lynden-Bell D., 1971, MNRAS, 155, 95
- Makiya R., Totani T., Kobayashi M., 2011, ApJ, 728, 158
- Petrosian V., 1992, in Feigelson E. D., Babu G. H., eds, Statistical Challenges in Modern Astronomy. Springer, New York, p. 173
- Shaw M. et al., 2012, ApJ, 748, 49
- Shaw M. et al., 2013, ApJ, 764, 135
- Singal J., Petrosian V., Ajello M., 2012, ApJ, 753, 45 (BP1)
- Singal J., Petrosian V., Stawarz Ł., Lawrence A., 2013, ApJ, 764, 43
- Singal J., Ko A., Petrosian V., 2014, ApJ, 786, 109
- Stecker F., Salamon M., 1996, ApJ, 464, 600
- Stecker F., Venters T., 2011, ApJ, 736, 40
- Venters T., Pavildou V., 2011, ApJ, 737, 80
- Venters T., Pavildou V., Reyes C., 2009, ApJ, 703, 1939
- Yonetoku D., Nakamura T., Yamazaki R., Inoue A., Ioka K., 2004, ApJ, 609, 935

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