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Quadrupole Collectivity in Neutron-Rich Fe and Cr Isotopes

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Intermediate-energy Coulomb excitation measurements are performed on the $N \geq 40$ neutron-rich nuclei ^{66,68}Fe and ⁶⁴Cr. The reduced transition matrix elements providing a direct measure of the quadrupole collectivity $B(E2; 2^+_1 \rightarrow 0^+_1)$ are determined for the first time in ⁶⁸Fe₄₂ and ⁶⁴Cr₄₀ and confirm a previous recoil distance method lifetime measurement in ${}^{66}Fe_{40}$. The results are compared to state-ofthe-art large-scale shell-model calculations within the full $fpgd$ neutron orbital model space using the Lenzi-Nowacki-Poves-Sieja effective interaction and confirm the results of the calculations that show these nuclei are well deformed.

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For many decades the nuclear shell structure originally proposed by Mayer [[1\]](#page-6-0) and Jensen and coworkers [[2\]](#page-6-1), where energy gaps are predicted at specific nucleon numbers, was a paradigm of nuclear physics, as it was consistent with the experimental findings at or near the valley of beta stability. However, with the possibility of producing more exotic nuclei, the traditional magic numbers have been observed to be weakened or to disappear while new subshell gaps have emerged. In particular, the role of the proton-neutron tensor interaction has been recognized as driving changes in the shell structure [[3](#page-6-2)]. Alterations to the effective single-particle orbital gaps can lead to enhanced particle-hole excitations, which are supported by deformation and pairing effects, and may give rise to new regions of well-developed nuclear deformation.

A region of recent interest is that of the neutron-rich isotopes near $N = 40$, below the ₂₈Ni isotopes. In many ways structurally similar to the "island of inversion" nuclei near $N = 20$ [\[4](#page-6-3)], the Fe and Cr isotopes in this region have been experimentally observed to exhibit increasingly collective behavior, rather than the near-magic behavior naively expected assuming a robust $N = 40$ subshell gap. In a schematic way, the development of collectivity moving from $_{28}$ Ni to $_{26}$ Fe and $_{24}$ Cr is understood as a result of a narrowing of the $N = 40$ subshell closure and the enhancement of quadrupole collectivity through promotion of neutron pairs across the subshell gap. With the removal of protons from the $1f_{7/2}$ orbital, the attractive tensor and central parts of the $p-n$ interaction between $1f_{7/2}$ proton holes and neutrons in the $1g_{9/2}$ and $2d_{5/2}$ orbits pull these neutron single-particle levels down in energy. At the same time, the repulsive tensor $(\pi 1 f_{7/2})^{-1} - \nu 1 f_{5/2}$ interaction dominates over the central
attractive n-n interaction and drives the neutron 1 f_{ata} orbiattractive p-n interaction and drives the neutron $1f_{5/2}$ orbital up, effectively quenching the $N = 40$ gap. Looking at it another way, adding 12 neutrons to 48 Ca produces a gapless ⁶⁰Ca; as protons are added in the $1f_{7/2}$ orbit, the repulsive interaction between the $1f_{7/2}$ protons and the $1g_{9/2}$ and $2d_{5/2}$ neutrons and the strongly attractive $\pi 1f_{7/2} - \nu 1f_{5/2}$
interaction opens the $N = 40$ gap up to its value in ⁶⁸Ni interaction opens the $N = 40$ gap up to its value in ⁶⁸Ni. The disappearance of the $N = 40$ gap towards ⁶⁰Ca supports the structural energy gain achieved by neutrons occupying the low- Ω substates of the $1g_{9/2}$ orbital, where Ω is the projection of the total angular momentum onto the symmetry axis [[5\]](#page-6-4), which drives the system towards deformed, collective structures. In other words, the quadrupole collectivity of the systems in the region is enhanced as a result of the nearby presence of the $\Delta j = 2$ partner orbitals
 $\frac{1}{2} \nu \sigma_{\text{e}}$ and $\frac{2}{\nu} d_{\text{e}}$ members of a quasi- $\frac{SI}{(3)}$ sequence $1\nu g_{9/2}$ and $2\nu d_{5/2}$, members of a quasi-SU(3) sequence,
which is known to generate quadrupole collectivity [6] which is known to generate quadrupole collectivity [[6\]](#page-6-5).

The picture of structural evolution described above is borne out by calculations using state-of-the-art large-scale shell-model calculations [\[7](#page-6-6)]. While the details of the predictions for the degree of collectivity vary between theoretical approaches, all available predictions place the midshell

 α_4^6 Cr nucleus at the center of the region of collectivity near $N = 40$. In this nucleus, deformation is maximized not only $N = 40$. In this nucleus, deformation is maximized not only by the increased population of the $g_{9/2}$ and $d_{5/2}$ neutron orbits, but also by the strong proton-neutron correlations which develop with four active protons in the fp shell [[7](#page-6-6)]. However, as is pointed out by Baugher *et al.* [\[8\]](#page-6-7), this maximum in deformation may not be completely robust, as they predict a saturation in deformation already reached in ⁶²Cr. The primary motivation of this work is the first direct measurement of the collectivity of the key nucleus, 64Cr.

Early measurements of the energy of the first 2^+ excited states in the Fe and Cr isotopes [\[9](#page-6-8)[–12\]](#page-6-9) showed a decreasing trend through $N = 40$, and recent lifetime measurements
in the neutron-rich ^{64,66}Ee isotones up to $N = 40$ [13,14] in the neutron-rich ^{64,66}Fe isotopes up to $N = 40$ [\[13](#page-6-10)[,14\]](#page-6-11)
have confirmed the collectivity in the Fe isotopes. In the have confirmed the collectivity in the Fe isotopes. In the lighter Cr isotopic chain, data are limited for $N \ge 40$. Coulomb excitation measurements provided collectivity data at $N = 32$ and 34 in the Cr isotopes [\[15\]](#page-6-12). The first (indirect) confirmation of increasing collectivity up to $N = 38$ was provided by proton inelastic scattering mea-surements [\[16\]](#page-6-13), recently confirmed by intermediate-energy Coulomb excitation probing the $B(E2)$ values directly [[8\]](#page-6-7). However, in ⁶⁴₄Cr the only experimentally available infor-
mation is $F(2^+)$ and $F(4^+)$ [10]; no measure of the extent mation is $E(2_1^+)$ and $E(4_1^+)$ [[10](#page-6-14)]; no measure of the extent
of collectivity is reported in the literature of collectivity is reported in the literature.

In addition to this first direct measurement of the collectivity of $_{24}^{64}$ Cr, we also present here confirmation of the measured quadrupole collectivity in $_{66}^{66}$ Fe [14] and an the measured quadrupole collectivity in ^{66}Fe [[14](#page-6-11)], and an extension of the $B(E2)$ systematics in the ₂₆Fe isotopic chain to ⁶⁸Fe at $N = 42$. Quadrupole collectivity was measured via determination of the $B(E2: 0^+_1 \rightarrow 2^+_1)$ or
reduced transition matrix elements using intermediatereduced transition matrix elements, using intermediate-energy Coulomb excitation [[17](#page-6-15)]. The measured $B(E2: 0^+_1 \rightarrow$ $_1$ \rightarrow
scale 2^{+}_{1}) values in ^{66,68}Fe and ⁶⁴Cr are compared with large-scale
shell-model calculations, providing a test of theory at the shell-model calculations, providing a test of theory at the center of this new ''island of inversion.''

The measurements were performed at the National Superconducting Cyclotron Laboratory at Michigan State University. Secondary radioactive ion beams containing 66Fe, 68Fe, and 64Cr were produced by in-flight fragmentation of a 130 MeV/A ⁷⁶Ge primary beam on a 399 mg/cm² ⁹Be foil production target. The fragments of interest were selected in the A1900 fragment separator $[18]$ using three separate magnetic rigidity settings for the three isotopes studied. In all cases, a 240 mg/cm² achromatic aluminum wedge degrader was located at the object position of the fragment separator, and the total momentum acceptance was restricted to 2% The resulting rare isotope beams had purities of 23% for ⁶⁶Fe, 6% for ⁶⁸Fe, and 2% for ⁶⁴Cr, with average rates of approximately 300, 20, and 2 particles per second incident on target, respectively.

Bismuth targets used to induce projectile Coulomb excitation were located at the target position of the S800 spectrograph [\[19](#page-6-17)] in the S3 experimental vault. Coulomb excitation of ⁶⁶Fe was studied using ²⁰⁹Bi targets of two

thicknesses, 245.2 and 492 mg/cm². Coulomb excitation of 68 Fe was studied with a target thickness of 245.2 mg/cm², while the measurement for ^{64}Cr used the thicker target of 492 mg/cm². The identification of the reaction residues was performed on an event-by-event basis utilizing the detection systems of the S800 focal plane [[20](#page-6-18)]. Energy loss was measured in an ionization chamber, while two xy-positionsensitive cathode-readout drift chambers provided position and angle information, and a plastic timing scintillator provided a stop for the time-of-flight measurement. The position and angle information at the target position was reconstructed using the information from the focal plane cathode-readout drift chambers, together with ion optics information for the S800. Reconstruction of the scattering angle on an event-by-event basis was critical to ensure selection of ''safe'' Coulomb excitation interactions. In intermediate-energy Coulomb excitation, due to the high bombarding energy, care must be taken to exclude nuclear contributions to the electromagnetic excitation process. This was accomplished by restricting the analysis to events at very forward scattering angles, which corresponded to large impact parameters, b. In this case, scattering angle upper limit cuts were made to ensure $b > b_{\min} = 1.2(A_{\text{target}}^{1/3} +$ $t \text{~}$ target ~ $A_{\text{projectile}}^{1/3}$ + 2 fm [[21\]](#page-6-19). Using the midtarget beam energies,
this positions corresponded to angle outs of Θ max this requirement corresponded to angle cuts of $\Theta_{\text{lab}}^{\text{max}}$ =
2.3° 2.5° 2.2° and 2.1° for the ⁶⁶Ee thin target the ⁶⁶Ee 2.3°, 2.5°, 2.2°, and 2.1° for the ⁶⁶Fe thin target, the ⁶⁶Fe thick target $68F$ _{Ee} and $64Cr$ respectively thick target, 68 Fe, and 64 Cr, respectively.

The reaction target in front of the S800 spectrograph was surrounded by CAESAR, an array of 192 CsI(Na) scintillator crystals for γ -ray detection [[22](#page-6-20)]. The high granularity of the array allowed for an event-by-event Doppler reconstruction, where the angle of the emitted γ ray was determined based on the position of the crystal recording the highest energy deposition in a given event. Covering approximately 95% of the solid angle, the singles photopeak efficiency of CAESAR was determined to be 30% at 1 MeV. Energy calibrations and photopeak efficiencies were determined with standard 22 Na, 60 Co, 137 Cs, and 88 Y sources, and compared with GEANT4 simulations which were used to model the response of the array. The simulations reproduced the measured source efficiencies of the setup to within 3%, which is included as a systematic error in the results.

The event-by-event Doppler-corrected γ -ray spectra obtained in coincidence with 66 Fe (245.2 mg/cm² target thickness), 68 Fe, and 64 Cr, satisfying the safe Coulomb excitation angle requirement, are shown in Fig. [1](#page-4-0). In each case, the only observed peak was the $2^{+}_{1} \rightarrow 0^{+}_{1}$ transition,
and the energies of these transitions agree well with the and the energies of these transitions agree well with the literature values [[10](#page-6-14)–[12](#page-6-9)]. To extract the number of γ rays emitted in each case, fits of the results of a GEANT4 simulation to the data were performed. The simulations account for the efficiency response of CAESAR, absorption in the target and include the calculated γ -ray angular distribution for the Coulomb excitation process [\[23](#page-6-21)[,24\]](#page-6-22). Overlaid on the experimental spectra in Fig. [1](#page-4-0) are the results of the fit,

FIG. 1 (color online). Doppler-corrected γ -ray spectra collected in coincidence with (a) ⁶⁶Fe, following Coulomb excitalected in coincidence with (a) ⁶⁶Fe, following Coulomb excita-
tion on the thin 245 mg/cm^{2 209}Bi target (b) ⁶⁸Fe, and (c) ⁶⁴Cr tion on the thin 245 mg/cm^{2 209}Bi target (b) ⁶⁸Fe, and (c) ⁶⁴Cr.
In each case, the spectra include γ rays in coincidence only with In each case, the spectra include γ rays in coincidence only with events detected in the S800 focal plane and scattering angles below the cutoff determined for safe impact parameters as described in the text. The fit of the GEANT simulation output (dot-dashed blue line) plus double exponential background (dashed green line) is shown in each case by the solid red line.

which included the GEANT4 simulated response function, plus a sum of two exponentials to represent the smooth background.

Angle-integrated Coulomb excitation cross sections to the first 2⁺ were determined and translated into $B(E2; 0^+_1 \rightarrow 2^+)$ values based on relativistic Coulomb excitation calcu- 2_{1}^{+}) values based on relativistic Coulomb excitation calcu-
lations performed following the formalism of Winther and lations performed following the formalism of Winther and Adler [\[24\]](#page-6-22), using RELEX [\[25](#page-6-23)]. The Coulomb excitation cross sections and extracted $B(E2)$ values are presented in Table [I](#page-4-1). The excitation cross sections include statistical uncertainties, uncertainties due to the fitting procedure used to extract the number of γ rays, and uncertainties in the simulated vs measured array efficiencies of 3% as described previously. In the case of ${}^{64}Cr$, the error in the simulated vs measured array response was estimated to be 6%, due to the low energy of the $2^+_1 \rightarrow 0^+_1$ transition, the sensitivity of the array response to detector thresholds, and sensitivity of the array response to detector thresholds, and the lack of a calibration point below 511 keV. The extracted $B(E2)$ values include an additional 5% uncertainty arising from the reconstruction of the scattering angle. The total error on the $B(E2)$ values presented in Table [I](#page-4-1) results from summing the contributing uncertainties in quadrature.

The present results confirm the previous recoil-distance method lifetime measurement and $B(E2)$ value in ⁶⁶Fe₄₀ as determined by Rother *et al.* $[14]$ $[14]$ $[14]$, with excellent agreement between the $B(E2)$ values determined using the two different 209Bi target thicknesses in the present measurement. The present results also extend the measured $B(E2)$ values for the Fe isotopic chain to $N = 42$ (⁶⁸Fe) and provide the first result at $N = 40$ in the . Cr chain first result at $N = 40$ in the ₂₄Cr chain.

Large-scale shell-model calculations provide one theoretical description of the region of $N = 40$ and have been successful in describing the low-energy structure of upper pf-shell nuclei. The Lenzi-Nowacki-Poves-Sieja (LNPS) effective interaction [\[7](#page-6-6)] assumes a ^{48}Ca core, and a valence space including the full *pf* shell for protons, and the $1f_{5/2}$, $2p_{3/2}$, $2p_{1/2}$, $1g_{9/2}$, and $2d_{5/2}$ single-particle states for neutrons. The interaction is tuned to reproduce the $N = 50$ shell closure behavior as observed in the $_{40}Zr$ isotopic chain and has shown good agreement with the excitation energies and $B(E2)$ values for the Fe and Cr isotopes approaching $N = 40$. The shell-model results using the LNPS effective interaction as presented in Ref. [\[7](#page-6-6)] are shown together with available experimental data down to $N = 32$ $N = 32$ in Fig. 2, including the present results [\[26](#page-6-24)–[28\]](#page-6-25).

As is evident in the top panel of Fig. [2,](#page-5-0) the LNPS effective interaction reproduces the energy of the first 2^+ excited states in the Fe and Cr chains quite well. However, the shell-model calculations appear to overestimate the magnitude of the quadrupole transition strengths using the standard polarization charge of $0.5e$ [\[8\]](#page-6-7). Using instead more realistic effective charges according to the Bohr-Mottelson formulation of the polarization charges, which

TABLE I. Angle-integrated Coulomb excitation cross sections and extracted $B(E2; 0^+_1 \rightarrow 2^+_1)$
values for ⁶⁶Fe (both target thicknesses) ⁶⁸Fe and ⁶⁴Cr values for ${}^{66}Fe$ (both target thicknesses), ${}^{68}Fe$, and ${}^{64}Cr$.

Isotopes	Target $(mg/cm2)$			σ (mb) $B(E2 \text{ } \uparrow)$ (e ² fm ⁴) Previous (e ² fm ⁴) LNPS (e ² fm ⁴)	
$^{66}_{26}Fe$	245.2 492	318(22) 331(30)	1455(124) 1430(149)	$1660(170)$ [14]	1680
$^{68}_{26}Fe$	245.2	388(43)	1777(216)	\cdots	1845
$^{64}_{24}Cr$	492	333(83)	1561(396)	\cdots	1805

FIG. 2 (color online). Systematics of $E(2_1^+)$ (upper panels) and
quadrupole collectivity (lower panels) along the Ee (left panels) quadrupole collectivity (lower panels) along the Fe (left panels) and Cr (right panels) isotopic chains. Shell-model calculations using the state-of-the-art LNPS [\[7\]](#page-6-6) effective interaction are shown by the solid red lines, using the effective charges of Dufour and Zuker [\[30\]](#page-6-27) and the nucleon valence spaces as described in the text for $N = 34$ through $N = 42$. For the calculations at $N = 32$, the neutron valence space excluded the $1g_{9/2}$ and $2d_{5/2}$ orbitals, but included the entire pf shell required for description of the lighter isotopes. Available experimental data are shown in hollow black symbols, including results deduced, with an optical model dependence, from (p,p') mea-surements [\[16\]](#page-6-13). The present results are shown as filled blue circles.

include isovector and isoscalar components [[29](#page-6-26)], the magnitudes of the calculated $B(E2)$ values are systematically reduced and the agreement of the calculated values with the experimental results, including the present result at ${}^{64}Cr$, are improved. Alternatively, recent investigations have shown that the use of the effective charges deduced by Dufour and Zuker [\[30](#page-6-27)], i.e., $e_{\pi} = 1.31e$ and $e_{\nu} = 0.46e$, without the need of including an isovector component, give an excellent need of including an isovector component, give an excellent description of the transition probabilities in different mass regions [\[31](#page-6-28)] and are compatible with the ones obtained in a recent fit of ^E2 properties of the sd shell with the USDA interaction [\[32](#page-6-29)]. We therefore adopt these effective charges and report the shell-model predictions shown by the solid red line in the bottom panels of Fig. [2.](#page-5-0)

It is worth emphasizing the importance of including the neutron $2d_{5/2}$ orbit in the valence space of the shell-model calculations, as is done in the calculations presented using the LNPS effective interaction. The inclusion of this orbital, a member of the quasi- $SU3$ sequence also containing the $1g_{9/2}$ orbit, is critical to building the quadrupole collectivity in the neutron-rich Fe and Cr isotopes [\[7](#page-6-6)], which calculations excluding this state fail to reproduce [[33](#page-6-30)].

It is also interesting to note that while no conclusions can be drawn looking at all the available data, the present results suggest larger collectivity in ${}^{68}Fe_{42}$ with respect

FIG. 3 (color online). Calculated proton and neutron electric quadrupole $(2^+_1 \rightarrow 0^+_1)$ transition amplitudes in e fm².

to ${}^{66}Fe_{40}$. The trend in the theoretical predictions is the same but smoother. In order to conclude that a nucleus has permanent deformation, it is necessary that both the $B(E2)$'s of the yrast band and the spectroscopic quadrupole moments can be obtained to a very good approximation from a single intrinsic deformed state. This is indeed the case in the calculations; for instance, in 64Cr this requirement is satisfied at the 3% level. The theoretical results can be interpreted in terms of the proton and neutron $E2$ transition amplitudes A_{π} and A_{ν} . The $B(E2)$ values and the intrinsic quadrupole moments are obtained from these the intrinsic quadrupole moments are obtained from these transition amplitudes by the expressions [\[7](#page-6-6)[,8](#page-6-7)]

$$
B(E2: 2_1^+ \to 0_1^+) = (e_\pi A_\pi + e_\nu A_\nu)^2, \tag{1}
$$

$$
Q_0 = \sqrt{16\pi B(E2 \, 1)} = \sqrt{16\pi} (e_{\pi} A_{\pi} + e_{\nu} A_{\nu}). \tag{2}
$$

As can be seen in Fig. [3](#page-5-1), the proton contribution to the $B(E2)$ values both in Cr and Fe isotopes is essentially constant, while the neutron contribution increases through $N = 38$ in the Cr isotopic chain. In the case of the Fe isotopes, the neutron contribution increases through $N = 40$, reproducing rather well the increase in $B(E2)$ value observed moving from ⁶⁶Fe to ⁶⁸Fe. Another point of note is that the measured $B(E2)$ value of ⁶⁸Fe is slightly larger than that of ${}^{64}Cr$, also in agreement with theory, although the error bars do not allow for a definite conclusion.

However, the issue of collectivity depends very much on the criteria chosen to gauge it. A measure of the ''nuclear'' collectivity is given by the intrinsic mass quadrupole moment

$$
Q_0(\text{mass}) = \sqrt{16\pi}q_m(A_\pi + A_\nu),\tag{3}
$$

to which neutrons and protons contribute with the same weight. With the effective mass $q_m = 1.77$ (the sum of the proton and neutron effective charges) and normalizing the calculated Q_0 's to $A = 64$ to remove the $A^{5/3}$ dependence of Q, within the framework of the shell-model calculations we obtain intrinsic mass quadrupole moments of 273, 318, 313, and 300 fm² for $60-66$ Cr, and 214, 243, 281, and 284 fm² for $62-68$ Fe. These calculations show a saturation of the deformation at $N = 38$ in the Cr chain, and at $N = 40$ in the Fe isotopes, as was noted in Ref. [[7](#page-6-6)]. Although marginally so, $62-64$ Cr are calculated to be the most deformed members of the island from the nuclear matter point of view, with $\beta = 0.3$, while in both the experiment and calculations 68 Fe has the largest $B(E2)$ value and electric intrinsic quadrupole moment.

In summary, we have studied the quadrupole collectivity in the neutron-rich $N \sim 40$ nuclei ^{66,68}Fe and ⁶⁴Cr via intermediate-energy Coulomb excitation. The present results provide a direct measure of the $B(E2; 0^+_1 \rightarrow 2^+_1)$
for the first time in ⁶⁸Fe, and ⁶⁴Cr, and confirm $\frac{1}{2}$ for the first time in ${}^{68}Fe_{42}$ and ${}^{64}Cr_{40}$, and confirm a
previous recoil-distance method lifetime measurement in previous recoil-distance method lifetime measurement in ${}^{66}Fe_{40}$. These new data in the most neutron-rich Fe and Cr isotopes provide a stringent test for state-of-the-art shellmodel theory. A comparison with calculations using the LNPS effective interaction show that the overall trend in $B(E2)$ values is well reproduced using realistic, universal effective charges. The calculations also show that nuclei in this region are well deformed, with maximum deformation in $62-64$ Cr or 68 Fe depending on the criteria chosen to define deformation. Extension of the $B(E2)$ systematics in this region, particularly in the $_{22}$ Ti isotopic chain below Cr, will be of interest as these isotopes become experimentally accessible, to confirm the true center of this region of deformation. Likewise, reaching further in neutron number towards the $N = 50$ spherical shell closure in the Cr and Fe isotopes will provide critical tests of the most advanced theoretical calculations.

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